# Origin of $\pi$-Facial Stereoselectivity in Nucleophilic Additions. Application of the Exterior Frontier Orbital Extension Model to Imines and Iminium Ions 

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The experimental data of $\pi$-facial stereoselection of the imines and the iminium ions of cyclohexanone, tropinone, and adamantan-2-ones have been explained by the exterior frontier orbital extension model (EFOE model) previously proposed. In all cases, facial difference in the $\pi$-planedivided accessible space (PDAS), which represents simple summation of the $\pi$-plane-divided exterior three-dimensional space nearest to the reaction center outside the van der Waals surface, significantly depends on the structure of the imino moieties. In particular the formation of iminium salt significantly affects the magnitude of both the EFOE density and the PDAS values.

## Introduction

Unraveling the mechanism and stereochemistry of addition reactions to $\pi$-bonds has attracted organic chemists' interests for over four decades and has been the subject of diverse investigations. ${ }^{1}$ Since Cieplak's proposal of his conceptual model in 1981,2 most discussions are focused on the importance of transition state stabilization arising from the anti-periplanar hyperconjugative stabilization effect involving the incipient bond. ${ }^{3}$ Recently we reported a quantitative analysis of the transition states of cyclohexanone reduction with Li$\mathrm{AlH}_{4 .}{ }^{4,5}$ It was proposed that the transition state effects, such as torsional strain and the anti-periplanar effect, are not essential for facial diastereoselection of nucleophilic additions to various cyclic ketones including ada-mantan-2-ones. Surprisingly they often operate against observed facial stereoselectivity. ${ }^{4}$

In the present paper, we extend our theoretical approach toward understanding the essential features of $\pi$-facial stereoselection based on the exterior frontier orbital extension model (the EFOE model) ${ }^{5,6}$ to the hydride reductions of the imines and iminium ions of cyclohexanone and tropinone and the oxonium ion of 5-fluoroadamantan-2-one.

## Computational Methods

The details of the definition of the two parameters of the EFOE model have been described elsewhere. ${ }^{5,6}$ The

[^0]EFOE model focuses on the first and third terms of the Salem-Klopman equation (eq 1). ${ }^{7}$

$$
\begin{aligned}
& \Delta E=-\underbrace{-\sum_{a b}\left(q_{a}+q_{b}\right) \beta_{a b} S_{a b}}_{\text {1st term }}+\underbrace{\sum_{k<l}^{\frac{Q_{k} Q_{l}}{r_{k l}}}}_{\text {2nd term }}+ \\
& \underbrace{\underbrace{\sum_{r}}_{\text {3rd term }}}_{\sum_{r} \sum_{s}-\sum_{s} \sum_{r} \underbrace{\text { occ. unocc. occ. unocc. } \underbrace{}_{a b} c_{r a} c_{s b} \beta_{a b})^{2}}_{E_{r}-E_{s}}} \\
& q_{a}, q_{b}=\text { electron density at atom } a \text { or } b . \\
& \beta=\text { resonance integral, } S=\text { overlap integral } \\
& Q_{k}, Q_{l}=\text { total electron densities at atom } k \text { or } l . \\
& r_{k l}=\text { distance between atoms } k \text { and } l . \\
& E_{r}=\text { energy level of MO } r . \\
& c=\text { MO coefficients }
\end{aligned}
$$

The model is designed for quantitative evaluation of the first (exchange repulsion; steric effects) and the third (orbital interaction; the donor-acceptor stabilizing interaction) terms to identify essential factors of $\pi$-facial diastereoselectivity of addition reactions to $\pi$-systems in general including ketones, alkenes, and enolates. Two new quantities-the $\pi$-plane-divided accessible space (PDAS) as the steric effect term and the exterior frontier

[^1]

Figure 1. Definition of the $\pi$-plane-divided accessible space (PDAS) for formal dehyde molecule.
orbital extension density (EFOE density) as the orbital interaction term-constitute the new model. Both quantities are defined in the exterior area ${ }^{8}$ of a molecule.

The definition of the PDAS is based on the simple assumption that the volume of the outer (exterior) space nearest to a reaction center should contain steric information of the reactant (substrate), since this volume precisely corresponds to the three-dimensional space available for a reagent to access the reaction center of the substrate. The exterior volume is calculated for the two faces of the $\pi$-plane separately. Figure 1 illustrates the definition of the $\pi$-plane-divided accessible space (PDAS) as a quantitative measure of $\pi$-facial steric effects using formaldehyde as an example. The molecular surface is defined as an assembly of spherical atoms having the appropriate van der Waals radii. ${ }^{9}$ Integration of the exterior three-dimensional space for the PDAS of the carbonyl carbon is performed according to the following conditions. If a three-dimensional point $\mathrm{P}(x, y, z)$ outside the repulsive surface is the nearest to the surface of the carbonyl carbon (a reaction center on the xz plane) (i.e., if the distance between $P$ and the van der Waals surface of the carbonyl carbon $\left(d_{C}\right)$ is the shortest compared with the distances from $P$ to the other atomic surfaces (two $d_{H}$ and one $\left.d_{O}\right)$ ) and if the point is located above the carbonyl plane ( $y>0$ ), the space at this point is assigned to the above-space of the carbonyl carbon. The integration (summation) of such points is defined as the PDAS of the carbonyl carbon for the above-plane. For the sake of convenience, spatial integration is limited to 5 au (2.65 $\AA$ ) from the molecular surface, where extension of an electronic wave function is negligible beyond this limit. In general, the carbonyl plane is defined as the plane which includes the two $\mathrm{sp}^{2}$ atoms of the $\pi$-bond and which is parallel with the vector connecting the two atoms at the $\alpha$-positions.

The third term parameter of the Salem-Klopman equation, namely the $\pi$-plane-divided EFOE density (hereafter called simply "EFOE density") is defined as the integrated (summed) electron density of a frontier orbital (FMO) ${ }^{10}$ over specific exterior points over oneface of the $\pi$-plane of a substrate molecule satisfying the following condition: the absol ute total value of the wave functions belonging to the carbonyl carbon makes a maximum contribution to the total value of FMO wave function at the point. Such a condition guarantees that the driving force vector on hydride or other reagent is

[^2]maximally directed toward the $\mathrm{sp}^{2}$ reaction center. Thus the integration of the FMO probability density ( $\Psi^{2}{ }_{\text {FMO }}$ ) over such three-dimensional subspace $(\Omega)$ that satisfies the above condition should afford a reasonable quantitative measure of the third term of eq 1 . The values of the EFOE density (eq 2) are expressed in \% for the sake of numerical convenience by normalizing the wave function ( $\Psi_{\text {Fмо }}$ ) to 100.
\[

$$
\begin{equation*}
\text { EFOE density }(\%)=100 \times \int \Psi_{\text {FMO }}^{2} \mathrm{~d} \Omega \tag{2}
\end{equation*}
$$

\]

The computer program was designed so that simultaneous calculation of both the PDAS and the EFOE density could be performed according to the threedimensional lattice method with a unit lattice volume of $0.008 \mathrm{au}^{3}\left(1.18 \times 10^{-3} \AA^{3}\right)$. The quality of each EFOE calculation was checked by the value of the total electron density of the FMO in interest, which converged nearly unity ( $1.000 \pm 0.001$ ). Spatial integration is limited to 5 au ( $2.65 \AA$ ) from molecular surface, where extension of an electronic wave function is negligible beyond this limit. The carbonyl plane is defined as the plane which includes both $\mathrm{sp}^{2}$ atoms of the $\pi$-bond and which is parallel with the vector connecting the two carbon atoms at the $\alpha$-positions. Bondi 's van der Waals radii ${ }^{9}$ were employed for the definition of molecular surface. The calculation procedure usually begins with structure optimization at the HF/6-31G(d) level using Gaussian 94 followed by a single point calculation with "gfinput" and "pop=full" keywords at the same level. ${ }^{11}$

## Results and Discussion

Remarkable predictive power of the EFOE model ${ }^{5,6}$ has been demonstrated in well-known examples of $\pi$-facial diastereoselectivity of carbonyl additions for which controversial arguments had been presented. ${ }^{1}$

We now report that the EFOE model can be successfully applied to imines and iminium ions as well. A number of reports have appeared to date on the facial stereoselection with respect to the $\mathrm{C}=\mathrm{N}$ bond in connection with the reductive amination of carbonyl compounds directed toward thetotal synthesis of natural products. ${ }^{12}$ Table 1 shows the EFOE analysis of LUMO's and observed stereoselectivities for some simple imines and imi nium ions of cyclohexanone (1) and the relevant data of cyclohexanones for comparison. On going from the

[^3]Table 1. EFOE Analysis of Cyclohexanone Imines and Iminium Ions (1) ${ }^{\text {a }}$

\begin{tabular}{|c|c|c|c|c|c|c|c|c|c|}
\hline \& \multirow[b]{2}{*}{\(\mathrm{R}_{1}\)} \& \multirow[b]{2}{*}{\(\mathrm{R}_{2}\)} \& \multicolumn{2}{|l|}{EFOE Density (\%)} \& \multicolumn{2}{|l|}{PDAS ( \(\mathrm{au}^{3}\) )} \& \multirow[t]{2}{*}{\[
\frac{\omega^{\mathrm{b}}}{\left(\mathrm{au}^{3}\right)}
\]} \& \multicolumn{2}{|l|}{obsd \({ }^{\text {c }}\)} \\
\hline \& \& \& ax \& eq \& ax \& eq \& \& reagents \& ax/eq \\
\hline \& \multicolumn{2}{|r|}{cyclohexanone} \& 1.940 \& 0.249 \& 19.4 \& 47.2 \& 27.8 \& \& \\
\hline \& \multicolumn{2}{|l|}{\multirow[t]{4}{*}{4-t-butylcyclohexanone}} \& \multirow[t]{4}{*}{1.799} \& \multirow[t]{4}{*}{0.249} \& \multirow[t]{4}{*}{19.6} \& \multirow[t]{4}{*}{46.7} \& \multirow[t]{4}{*}{27.1} \& \(\mathrm{LiAlH}_{4}\) \& 92:8 \({ }^{\text {e }}\) \\
\hline \& \& \& \& \& \& \& \& \[
\mathrm{NaBH}_{4}
\] \& 83:17 \({ }^{\text {f }}\) \\
\hline \& \& \& \& \& \& \& \& \[
\mathrm{NaBH}_{3} \mathrm{CN}
\] \& 84:16 \({ }^{\text {f }}\) \\
\hline \& \& \& \& \& \& \& \& \(\mathrm{AlH}_{2}\left(\mathrm{OR}^{\prime}\right)_{2} \mathrm{Na}^{\text {d }}\) \& 92:8f \\
\hline \multirow[t]{2}{*}{imines (1a)} \& \multicolumn{2}{|l|}{\multirow[t]{2}{*}{\[
\begin{aligned}
\& \mathrm{H} \\
\& \mathrm{Me}
\end{aligned}
\]}} \& 1.367 \& 0.168 \& 14.7 \& 49.8 \& 35.1 \& \& \\
\hline \& \& \& 1.313 \& 0.175 \& 13.3 \& 46.6 \& 33.3 \& \& \\
\hline \multirow[t]{11}{*}{iminium ions (1a)} \& \multirow[t]{5}{*}{\begin{tabular}{l}
H \\
Me
\end{tabular}} \& \multirow[t]{5}{*}{\[
\begin{aligned}
\& \mathrm{H} \\
\& \mathrm{Me}
\end{aligned}
\]} \& 1.170 \& 0.631 \& 14.0 \& 45.5 \& 31.4 \& \& \\
\hline \& \& \& \multirow[t]{4}{*}{1.176} \& \multirow[t]{4}{*}{0.763} \& \multirow[t]{4}{*}{11.0} \& \multirow[t]{4}{*}{42.2} \& \multirow[t]{4}{*}{31.2} \& \(\mathrm{LiAlH}_{4}\) \& 65:35 \\
\hline \& \& \& \& \& \& \& \& \[
\mathrm{NaBH}_{4}
\] \& 84:16 \({ }^{\text {f }}\) \\
\hline \& \& \& \& \& \& \& \& \(\mathrm{NaBH}_{3} \mathrm{CN}\) \& 58:42 \({ }^{\text {f }}\) \\
\hline \& \& \& \& \& \& \& \& \(\mathrm{AlH}_{2}\left(\mathrm{OR}^{\prime}\right)_{2} \mathrm{Na}^{\text {d }}\) \& 28:72 \({ }^{\text {f }}\) \\
\hline \& \multirow[t]{6}{*}{\(\mathrm{CH}_{2} \mathrm{Ph}\)
(py

(p)} \& \multirow[t]{2}{*}{H} \& \multirow[t]{2}{*}{1.270} \& \multirow[t]{2}{*}{0.618} \& \multirow[t]{2}{*}{13.7} \& \multirow[t]{2}{*}{38.1} \& \multirow[t]{2}{*}{24.4} \& $\mathrm{NaBH}_{3} \mathrm{CN}$ \& 65:359 <br>
\hline \& \& \& \& \& \& \& \& $\mathrm{NaBH}(\mathrm{OAC})_{3}$ \& 20:80h <br>

\hline \& \& \multirow[t]{3}{*}{$$
\begin{gathered}
-\left(\mathrm{CH}_{2}\right)_{4}- \\
\text { (pyrrolidinium) }
\end{gathered}
$$} \& \multirow[t]{3}{*}{1.286} \& \multirow[t]{3}{*}{0.691} \& \multirow[t]{3}{*}{12.4} \& \multirow[t]{3}{*}{37.5} \& \multirow[t]{3}{*}{25.1} \& $\mathrm{NaBH}_{4}$ \& 86:14 ${ }^{f}$ <br>

\hline \& \& \& \& \& \& \& \& $\mathrm{NaBH}_{3} \mathrm{CN}$ \& 64:36 ${ }^{\text {f }}$ <br>

\hline \& \& \& \& \& \& \& \& $\mathrm{AlH}_{2}\left(\mathrm{OR}^{\prime}\right)_{2} \mathrm{Na}^{\text {d }}$ \& $$
30: 70^{f}
$$ <br>

\hline \& \& $$
\begin{gathered}
-\left(\mathrm{CH}_{2}\right)_{5}- \\
\text { (piperidinium) }
\end{gathered}
$$ \& 0.926 \& 0.806 \& 9.2 \& 23.1 \& 13.9 \& $\mathrm{LiAlH}_{4}$ \& 64:36 <br>

\hline
\end{tabular}

${ }^{\text {a }} \mathrm{HF} / 6-31 \mathrm{G}(\mathrm{d}) ; \mathrm{R}=\mathrm{H}$ unless otherwise noted. ${ }^{\mathrm{b}} \omega=$ PDAS(eq) - PDAS(ax). ${ }^{\mathrm{c}}$ tert-Butylcyclohexanone imine ( $\mathbf{l b}$ ) $(\mathrm{R}=\mathrm{t}-\mathrm{Bu}) .{ }^{\mathrm{d}} \mathrm{R}^{\prime}=$ $\mathrm{CH}_{2} \mathrm{CH}_{2} \mathrm{OCH}_{3}$. ${ }^{e}$ Reference 12 c . ${ }^{\dagger}$ Reference 12b. ${ }^{9}$ Reference 12 a . ${ }^{\mathrm{h}}$ Reference 12 g .

Table 2. EFOE Analysis of the Imines and Iminium Ions of Model Tropinone ( 2 m ) and Observed Stereoselection of Tropinone (2) ${ }^{\text {a }}$

| 2m |  | EFOE Density (\%) |  | PDAS ( $\mathrm{au}^{3}$ ) |  | $\omega\left(\mathrm{au}^{3}\right)^{\mathrm{b}}$ | reagent | obsd for (2) exo:endo |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{R}_{1}$ | $\mathrm{R}_{2}$ | exo | endo | exo | endo |  |  |  |
| tropinone |  | 0.175 | 1.431 | 36.1 | 8.9 | 27.2 | - | - |
| H | - | 0.143 | 0.672 | 42.7 | 5.4 | 37.3 | - | - |
| Me | - | 0.127 | 1.019 | 33.5 | 6.3 | 27.2 | - | - |
| H | H | 0.469 | 0.852 | 30.8 | 8.2 | 22.6 | - | - |
| Me | H | 0.409 | 1.128 | 25.8 | 10.6 | 15.2 | - | - |
| Me | Me | 0.382 | 1.507 | 24.5 | 18.2 | 6.3 | - | - |
| $\mathrm{PhCH}_{2}{ }^{\mathrm{c}, \mathrm{d}}$ | - | 0.161 | 0.793 | 36.2 | 5.3 | 30.9 | $\begin{aligned} & \mathrm{NaBH}(\mathrm{OAC})_{3} \\ & \mathrm{NaBH}_{4}{ }^{\mathrm{e}} \end{aligned}$ | $\begin{aligned} & 20: 1^{f} \\ & 1.5: 1^{f} \end{aligned}$ |
| $\mathrm{MeOCOCH} 2{ }^{\text {c }}$ | - | 0.873 | 0.201 | 31.9 | 4.8 | 27.1 | $\mathrm{NaBH}(\mathrm{OR})_{3}{ }^{\text {g }}$ | 100:0h |
| $\mathrm{Ph}^{\mathrm{c}, \mathrm{d}}$ | - | 0.425 | 0.128 | 18.5 | 5.3 | 13.2 | $\mathrm{NaBH}(\mathrm{OAC}) 3$ | 100:0f |
| piperidine |  | 0.503 | 1.197 | 17.5 | 30.3 | -12.8 | $\mathrm{NaBH}_{4}{ }^{\text {e }}$ | 1:7 ${ }^{\text {f }}$ |
| piperazine |  | 0.507 | 1.116 | 19.0 | 27.8 | -8.8 | $\mathrm{NaBH}_{4}{ }^{\text {e }}$ | 1:15 ${ }^{\text {h }}$ |

${ }^{\text {a }} \mathrm{HF} / 6-31 \mathrm{G}(\mathrm{d}) .{ }^{\mathrm{b}} \omega=$ PDAS(exo) - PDAS(endo). ${ }^{\mathrm{c}}$ The most stable conformer was selected. ${ }^{\mathrm{d}} \mathrm{LUMO}+2$. ${ }^{\mathrm{e}} \mathrm{I}$ n the presence of $\mathrm{Ti}\left(\mathrm{O}^{\mathrm{i}} \mathrm{Pr}\right)_{4}$. ${ }^{\mathrm{f}}$ Reference $12 \mathrm{e} .{ }^{\mathrm{g}} \mathrm{R}=2$-ethoxyhexanoyl. ${ }^{\mathrm{h}}$ Reference 13.
ketone to the NR ( $\mathrm{R}=\mathrm{H}, \mathrm{Me}$ ) imines, both the PDAS values and the EFOE densities for the ax-face decrease ( $\sim 19 \rightarrow \sim 13$ au $^{3} ; \sim 1.9 \rightarrow \sim 1.3 \%$ ). On going from the imines to the iminium ions ( $\left(\mathrm{R}_{1}, \mathrm{R}_{2}\right)=\mathrm{H}$ or Me$)$, the PDAS values for the axial face (ax-face) further decrease ( $14-13 \rightarrow 14-9$ au $^{3}$ ), while the EFOE density values for the equatorial face (eq-face) significantly increase ( $\sim 0.2$ $\rightarrow \sim 0.7 \%$ ). This is consistent with the observed facial stereoselectivity of the iminium ions listed in Table 1 which shows enhanced equatorial selectivities compared with 4 -tert-butylcyclohexanone in hydride reduction. It is noted that the stereochemical changes may originate from the skeletal deformation of the iminium ions arising from the hybridization changes of the $\alpha$-carbons toward $\mathrm{sp}^{2}$ owing to the enhanced electron demand from the electron-deficient iminium carbon (hyperconjugation), which is much more electron-deficient than the $\mathrm{C}=\mathrm{N}$ bond of the imines. For example, comparison between the NH imine ( $\mathbf{1} ; \mathrm{R}_{1}=\mathrm{H}, \mathrm{R}_{2}=$ lone pair) and the $\mathrm{NH}_{2}$ iminium ion of cyclohexanone ( $\mathbf{1} ; \mathrm{R}_{1}=\mathrm{H}, \mathrm{R}_{2}=\mathrm{H}$ ) reveals simultaneous bond shortening of C1-C2 (C1-C6) (1.516 $\rightarrow 1.495 \AA$ ) and bond elongation of $\mathrm{C}=\mathrm{N}(1.256 \rightarrow 1.281$ A) due to the hyperconjugation between the $\pi_{\mathrm{C}=N^{*}}$ and $\mathrm{C} 1-\mathrm{H}(\mathrm{C} 6-\mathrm{H})$ bonds.

This seems the trend commonly observed for the iminium ions of tropinone (2) as described below. Table

2 collects the EFOE data of the imines and the iminium ions of model tropinone ( $\mathbf{2 m}$ ), in which the N -methyl is replaced by hydrogen for computational convenience, along with some experimentally determined stereoselectivity of the reductive amination of tropinone with various amines. In complete agreement with the EFOE data, it has long been known that the hydrogenation of parent tropinone occurs from the less-hindered exo-face to give the endo al cohol, whereas $\mathrm{LiBH}_{4}$ reduction takes place preferentially from the endo-face: the endo-face of model tropinone is much more sterically congested (PDA$\mathrm{S}($ exo $\left.)=8.9 \mathrm{au}^{3}\right)$ than the exo-face $($ PDAS (endo) $=36.1$ $\mathrm{au}^{3}$ ), whereas the EFOE density of model tropinone for the same face ( $1.431 \%$ ) is much greater than that of the other face ( $0.175 \%$ ).
The EFOE analysis of the imines and the iminium ions of model tropinone ( $\mathbf{2 m} ; \mathrm{R}_{1}, \mathrm{R}_{2}=\mathrm{H}, \mathrm{Me}$ or lone pair) show some interesting features. The imines show analogous trends as model tropinone itself. However, the iminium ions exhibit two notable changes due to considerable skeletal deformation due to enhanced hyperconjugation: the endo-face becomes less hindered due to enhanced coplanarity around $\mathrm{C}-2, \mathrm{C}-3$, and $\mathrm{C}-4$, while the endo/ exo ratio of the EFOE density increases. Indeed, as the methyl substitution increases in the iminium ions ( $\mathrm{C}=$ $\mathrm{NH}_{2} \rightarrow \mathrm{C}=\mathrm{NHMe} \rightarrow \mathrm{C}=\mathrm{NMe}_{2}$ ), the PDAS values for the

(a) Iminium

(b) Methyl Iminium

(c) Dimethyl Iminium

Figure 2. Side views of the optimized structures and the PDAS values of (a) iminium, (b) methyliminium, and (c) dimethyliminium ions of the model tropinone ( $\mathbf{2 m}$ ) (HF/6-31G(d)).

Table 3. EFOE Analysis of Danishefsky Imine (3), Adamantanone Oxonium (4), Imine (5), and Iminium Ion (6)a

| compd no. | EFOE Density (\%) |  | PDAS ( $\mathrm{au}^{3}$ ) |  | $\omega\left(\mathrm{au}^{3}\right)^{\mathrm{b}}$ | bond length ( $\AA$ ) |  | obsd A:B |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | A | B | A | B |  | C1-C2 | C2-C3 |  |
| 3 | 0.222 | 1.075 | 4.2 | 9.3 | 5.1 | - | - | 0:100 ${ }^{\text {c }}$ |
| adamantan-2-one | 1.097 | 1.098 | 11.1 | 11.1 | 0.0 | 1.5246 | 1.5246 | 50:50 |
| 5-F-adamantan-2-one | 1.032 | 1.068 | 10.3 | 12.7 | 2.4 | 1.5271 | 1.5271 | 38:62 ${ }^{\text {d }}$ |
| 4 | 0.929 | 1.236 | 7.5 | 11.1 | 3.6 | 1.4927 | 1.4934 | 17:83e |
| 5 | 0.793 | 0.746 | 9.0 | 9.8 | 0.8 | 1.5183 | 1.5238 | - |
| 6 | 0.825 | 0.911 | 8.4 | 9.7 | 1.3 | 1.5138 | 1.5139 | - |

${ }^{\text {a }} \mathrm{HF} / 6-31 \mathrm{G}(\mathrm{d}) .{ }^{\mathrm{b}} \omega=\mathrm{PDAS}(\mathbf{B})-\operatorname{PDAS}(\mathbf{A}) .{ }^{\mathrm{c}}$ Reduction with $\mathrm{NaCNBH}_{3}$. Reference 14. ${ }^{\mathrm{d}}$ Reduction with $\mathrm{NaBH}_{4}$. Reference 3 . e Reduction with $\mathrm{NaBH}_{4}$. Reference 15.
endo-face increase ( $8.2 \rightarrow 10.6 \rightarrow 18.2 \mathrm{au}^{3}$ ). Simultaneously the endo/ exo ratio of EFOE density increases. It follows that alkyl substitution at the nitrogen of an iminium ion of tropinone should activate the endo-face both sterically and electronically. As shown in Figure 2, this changes correspond to the increase in hyperconjugation of methyl as indicated by the increase of the torsion angle between C3 $=\mathrm{N}$ and $\mathrm{C} 2(\mathrm{C} 4)-\mathrm{H}_{\text {exo }}$ bonds (95.0 $\rightarrow 90.0 \rightarrow 74.9^{\circ}$ ) as methyl substitution increases at the nitrogen.


As shown in the last six experimental data of hydride reductions of the imines and the iminium ions listed in Table 2, stereochemical control of the reductive amination of tropinone has been achieved by the use of amines with bulky substituents. The imines of benzylamine, ${ }^{12 e}$ glycine, ${ }^{13}$ and aniline ${ }^{12 e}$ effectively completely block the endoface (PDAS(endo) $=\sim 5 \mathrm{au}^{3}$ ) and reduce the EFOE density of the endo-face to undergo preferentially the exoattack, while secondary amines, such as piperidine ${ }^{12 e}$ or piperazine, ${ }^{13}$ make the endo-face much less hindered and more reactive as predicted not only by the PDAS values of the piperidinium and piperazinium ions (PDAS (endo)

[^4]
(a) Piperidinium

(b) Piperazinium

Figure 3. Side views of the optimized structures and the EFOE data of (a) the piperidinium ion and (b) the piperazinium ion of the model tropinone (2m). Numbers in \% are the EFOE density and PDAS values are indicated in parentheses.
$=30.3$ and 27.8 au $^{3}$, respectively) but also by the EFOE densities of the endo-face ( 1.197 and $1.116 \%$, respectively) to give the endo products predominantly. ${ }^{13}$ As shown in Figure 3, the torsion angle between $\mathrm{C} 3=\mathrm{N}$ and $\mathrm{C} 2(\mathrm{C} 4)-$ $\mathrm{H}_{\text {exo }}$ bonds of the structures of these two iminium ions optimized at the HF/6-31G(d) level are only $64.8^{\circ}$ and $66.6^{\circ}$ for the piperidinium and piperazinium ions, respectively, to make the three-carbon bridge (C1-C2-C3-C4-C5) nearly coplanar with the $\mathrm{C}=\mathrm{N}$ bond. This strongly indicates that conformational deformation due to hyperconjugation is responsible for the remarkable change of facial stereoselection for these iminium ions.

A few interesting examples of facial selection of imines, oxonium ions, and iminium ions have been recently reported. ${ }^{14,15}$ Table 3 collects the results of the EFOE analysis. Tricyclic imine (3), prepared as an intermediate for the total synthesis of naturally occurring phospholipase inhibitor hispidospermidine, undergoes exclusive equatorial hydride reduction upon treatment with sodium cyanoborohydride. ${ }^{14}$ Danishefsky correctly predicted "relatively unencumbered" equatorial face (face "B" indi cated

[^5]in structure 3) to be more preferred. In agreement with his intuition, the EFOE data show that both EFOE density and PDAS value prefer equatorial attack from face "B" at 3.


3


4


5


6

Very recently, le Noble et al. reported the stereochemistry of hydride reduction of adamantan-2-one oxonium ion and some related systems. ${ }^{15}$ Enhanced syn stereochemistry of $\mathrm{NaBH}_{4}$ reduction of 2-(2-methoxy-5-fluoro-
adamantyl) cation (4) (anti:syn $=17: 83$ ) was observed. le Noble attributed this enhancement of syn-face sel ection compared with that of 5-fluoroadamantan-2-one (anti :syn $=37: 63 ; \mathrm{NaBH}_{4}$ reduction) ${ }^{3 a}$ to the increase of electrondemand of the carbonyl oxygen. The EFOE analysis shows significant skeletal deformation in cations 4 ( $\omega=$ 3.6) owing to some shrinkage of C1-C2 and C2-C3 bonds $(1.527 \rightarrow 1.493 \AA$ ) compared with those of 5 -fluoroada-mantan-2-one ( $\omega=2.4$ ). As a result, face " $B$ " is more activated toward reduction both sterically and electronically. The data of the EFOE analysis of imine 5 and iminium ion 6 were also collected for comparison.

In conclusion, the EFOE analyses of the imines and iminium ions of cyclohexanone and tropinone have revealed that the facial stereoselection of these systems is most likely to be dictated by steric effect and by the extension of LUMO. It was found that the ground-state skeletal deformation arising from the enhanced resonance effect in iminium ions is most likely to be responsible for the changes of facial stereoselection of nucleophilic additions to the systems studied.

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